# Processing-microstructureproperty relationships

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# Introduction

- Grain size control
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25 20 G (10<sup>6</sup> K/m) 15 10

## Distance from the bottom of melt pool ( $\mu$ m)



Fig. Thermal gradient (G) variation with distance form the bottom of the melt pool

(R: solidification speed, G:Thermal gradient)

**Fig.** Expected microstructures resulting from (R: solidification speed, G:Thermal gradient)



# *R* (m/s)

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Mishra and Thapliyal 2021 [https://doi.org/10.1016/j.matdes.2021.109640]



**Fig.** Typical variation in temperature for Subsequent printed layers L1, L2, ...

Source: Kirka et al. 2017 [http://dx.doi.org/10.1016/j.scriptamat.2017.01.005]



**Fig.** Typical temperature variation at a given point in the subsurface **Note:** the time axis is shifted as the laser is approximately approaching the reference point



Source: Liu et al . 2022 [https://doi.org/10.1016/j.jmst.2021.06.011]



Fig. Schematics of dislocation cell formation during AM thermal cycling

Source: Liu et al . 2022 [https://doi.org/10.1016/j.jmst.2021.06.011]

### Disordered dendrites/cells



Fig. Typical dislocation cell structures formed at various stages of heating and cooling

Source: Sabzi et al. 2021 [https://doi.org/10.1016/j.matdes.2021.110246]

**Fig.** Variation of recovery, continuous (CDRX) And discontinuous dynamic recrystallization (DDRX) at various strain stages and for various Strain rates

Where,

 $\dot{\varepsilon}$  : strain rate

 $\dot{\varepsilon}_c^T$ : critical strain rate for Dynamic recrystallization activation

 $\varepsilon_c^{c/T}$ : critical strain for the Formation of highangle grain boundaries



Source: Sabzi et al. 2021 [https://doi.org/10.1016/j.matdes.2021.110246]



Fig. Remelting stages influence on substructure formation

Source: Karimi et al. 2021 [https://doi.org/10.1016/j.addma.2021.102086]

**Fig.** Influence of build direction on Microstructural orientation (a) Sample SS-0, (b) sample SS-90, and (c) sample SS-67, and (d) volume fraction of recrystallization.



Source: Xu et al. 2021 [https://doi.org/10.1016/j.matdes.2021.109940]



Source: Gatsos et al. 2020 [https://doi.org/10.1007/s11837-019-03913-x]

# **Modelling approaches**



Fig. Description of element configurations in meting stages

Source: Tan et al. 2020 [https://doi.org/10.1080/17452759.2019.1677345]

## **Residual stress and distortion equations**

$$\nabla \cdot \sigma = 0$$
$$\sigma = C\epsilon$$

$$\epsilon = \epsilon_e + \epsilon_p + \epsilon_T + \epsilon_V$$

$$\epsilon_T = \alpha_{CTE} (T - T_{ref})$$

σ: residual stressε: distortionC: stiffness tensor

 $\epsilon_e$ : elastic strain  $\epsilon_p$ : plastic strain  $\epsilon_T$ : thermal strain  $\epsilon_v$  thermal strain due to phase transformations

 $\alpha_{\text{CTE}}$  :coefficient of thermal expansion  $T_{\text{ref}}$  : is the reference temperature

# **Modelling approaches**

## Microstructure Models

## Phase Field Method Boundary conditions:

- Initial temperature
- Temperature gradient
- Melt pool angle
- Fluid flow
- Nucleation density
- Seeded dendrite angles Assumptions:
- Growth from seeded round dendrites
- Material reduced to binary alloy

## Kinetic Monte Carlo Boundary conditions:

- Melt pool temperature
- Melt pool shape

#### Assumptions:

 Lowest energy state of each time step is the resultant microstructure

## Cellular Automata

#### Boundary conditions:

- Melt pool temperature
- Melt pool shape
- Nucleation density
- Seeded grain angles

#### Assumptions:

- Solidification theory holds for given thermal profile
- Dendrites grow in the <100> direction

# Modelling approaches – Phase field simulations of orientation



Fig. Accuracy of Phase field simulation for grain morphology and orientation

Source: Park et al. 2020 [https://doi.org/10.1016/j.matdes.2020.108985]

# Phase field modelling equations

$$\frac{\partial \phi}{\partial t} = L \frac{\partial F}{\partial \phi}$$

$$F = \int \left[ f_0(\phi, T) + \frac{1}{2} \kappa_{\phi} (\boldsymbol{\nabla}\phi)^2 \right] dV$$

$$f_0 = hf^S + (1-h)f^L + Qf$$

$$\kappa_{\phi} = \frac{9\gamma^2}{32\Delta f}$$

F: microstructure free energy functional L: kinetic rate coefficient

f<sub>0</sub> ( $\phi$ , T):local free energy density, V: volume,  $\kappa_{\phi}$ : gradient energy coefficient.

f<sup>s</sup> and f<sup>L</sup> : free energies of the solid and liquid phases, respectively,Q: height of the activation barrier at the interface,

h = 
$$\phi^2(3-2\phi)$$
, and

 $f = \phi^2 (1 - \phi)^2$ 

 $\gamma$ : specific interfacial energy (interfacial energy per unit area)

# **Monte Carlo mathematical formulation**

$$P = \exp\left(-\frac{\Delta E}{k_B T_s}\right), \quad \text{if} \quad \Delta E > 0 \qquad P: \text{acceptance probability}$$

$$k_{\text{B}}: \text{Boltzmann constant,}$$

$$k_{\text{B}}T_{\text{s}}: \text{thermal fluctuation during simulation,}$$

$$P = 1, \quad \text{if} \quad \Delta E \le 0 \qquad \Delta E: \text{overall system energy change}$$

# **Modelling approaches**

**Fig.** Comparison of AMed experimental and MC simulated microstructures on IN718 showing a good agreement



Source: Rodgers et al. 2017 [https://doi.org/10.1016/j.commatsci.2017.03.053]

# **Cellular automata equations**

$$n(\Delta T) = \int_{0}^{\Delta T} \frac{dn}{d(\Delta T)} d\Delta T$$
$$\frac{dn}{d(\Delta T)} = \frac{n_{max}}{\sqrt{2\pi}} \exp\left[-\frac{(\Delta T - \Delta T_{mean})}{2\Delta T_{\sigma}}\right]$$
$$\Omega = \frac{C^* - C_0}{C^*(1 - K)} = \operatorname{Iv}\left(\frac{\operatorname{VR}}{2\operatorname{D}}\right)$$
$$R = 2\pi \sqrt{\frac{\Gamma}{mG_c\xi_c - G}}$$
$$\xi_c = \frac{\pi^2}{K(\frac{\operatorname{VR}}{2\operatorname{D}})^2}$$
$$\Delta T = mC_0 \left(1 - \frac{1}{\Omega(1 - K)}\right)$$

ΔT: liquid undercooling

n: Continuous grain density

n<sub>max</sub>: maximum nucleation density,

 $\Delta T_{mean}$ : mean undercooling when nucleation occurs

 $\Delta T_{\sigma}$ : standard deviation of the undercooling

 $\Omega$ : solute supersaturation,

C\*: liquid solute concentration at the dendrite tip,

Co: initial solute concentration,

V: growth speed of the dendrite tip,

R: radius of the dendrite tip,

D:solute diffusion coefficient,

lv :lvantsov's solution,

K: partition coefficient,

m: liquidus slope,

Γ: Gibbs-Thomson coefficient,  $\xi_c$ 

Gc: solute gradient,

G: temperature gradient,

ΔT: undercooling temperature

# Summary



Fig. Integration of processing-microstructure-properties modelling in AM

Source: Grilli et al. 2022 [https://doi.org/10.1007/s00466-021-02116-z]